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Sylvain Patinet, Daniel Bonamy, L Proville. Atomic-scale avalanche along a dislocation in a random alloy. *Physical Review B: Condensed Matter and Materials Physics* (1998-2015), 2011, 10.1103/PhysRevB.84.174101 . hal-01224256

HAL Id: hal-01224256

<https://hal.science/hal-01224256>

Submitted on 6 Nov 2015

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Atomic-scale avalanche along a dislocation in a random alloy

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The propagation of dislocations in random crystals is evidenced to be governed by atomic-scale avalanches whose the extension in space and the time intermittency characterizingly diverge at the critical threshold. Our work is the very first atomic-scale evidence that the paradigm of second order phase transitions applies to the depinning of elastic interfaces in random media.

PACS numbers: 62.25.-g, 45.70.Ht, 61.72.Lk, 64.70.qj

INTRODUCTION

Avalanche like motion of isolated elastic interfaces in random media is a process now clearly recognized at laboratory scales, e.g. in Barkhausen effect [1], brittle fracture [2] imbibition [3], etc. Mesoscale scalar field theory [4] captures such a behavior and allows theoreticians to define an universal critical behavior close to the depinning threshold, with a divergence of mean avalanche extents and durations. Though, the field theory remains limited to a realm by far larger than the atomic-scale. This is due to a prerequisite coarse-graining which introduces an averaging distance cutoff much larger than the typical inter-atomic distances.

Here we show that the critical avalanching behavior predicted throughout field theory is still a concern at the atomic-scale, along an isolated dislocation moving in a random crystal. Dislocations exhibit morphological scaling features. They also propagate through jerky avalanches, the size and duration of which are power-law distributed up to a cut-off which diverges as the critical stress is approached. All the scaling relations expected from the standard depinning theory are fulfilled down to the atomic scale.

NUMERICAL METHODS

Plastic deformation of a solid solution is a prototypical example where dislocations must pass a random distribution of atomic-size obstacles to release plastic flow [5]. Despite the most recent progresses in tunneling electron microscopy [6], it is practically unfeasible for experiments to analyze selectively a dislocation depinning and its associated roughness, at the atomic scale. Hence numerical simulations are resorted to, as they enable us to focus on the dynamics of a single dislocation. Molecular dynamics (MD) simulations are employed in order to integrate the degrees of freedom of the whole crystal with atomic size impurities. The main advantage of MD simulations is that the dislocation is not modeled by a phenomenological elastic manifold [7–9] but more realistically as a

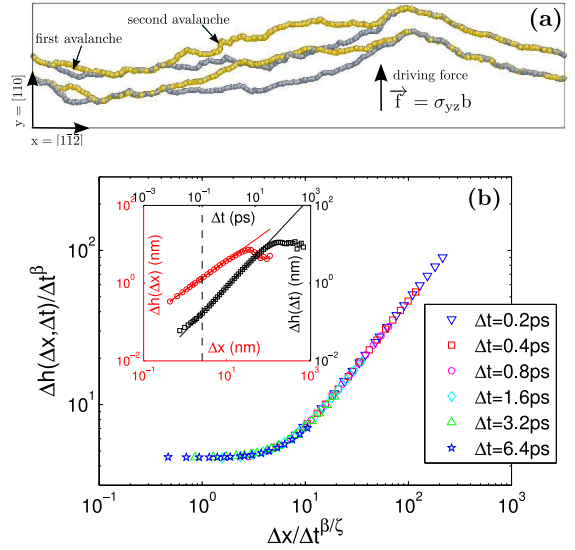


FIG. 1. (Color online) (a) Plane view for an edge dislocation at two different times in Ni(Al) alloy, modeled within EAM Ref.[10]. Only Shockley partial dislocation core atoms are colored before (gray) and after (yellow) a sequence of two avalanches separated by 10 ps. The rest of the crystal atoms are not shown. (b) Main panel: Collapsed space-time height-height correlation function $\Delta h/\Delta t^\beta$ vs. $\Delta x/\Delta t^{\beta/\zeta}$ at various Δt obtained at $\sigma_{yz} = 171.2$ MPa with $\zeta = 0.85$ and $\beta = 0.76$ obtained from the fits in inset. Inset: space (circles) and time (squares) height-height correlation function. Straight lines are power-law fits. The vertical dashed line corresponds to the lower time cutoff.

Burgers discontinuity in the atom arrangement. Note also that this method ensures a proper inclusion of the non-linearities governing the dislocation self-interactions and a time scale with clear physical meaning.

Typical snapshots of the dislocation position at two successive times are shown in Fig. 1 (a). A single-crystal of binary Ni(Al) solid solutions (10 atomic percent of Al randomly distributed in the Ni matrix) with a single [110] edge dislocation is deformed under a constant shear stress at 5 K. The technical details of these MD simulations can

be found in [10] and briefly recalled hereafter.

The interactions between atoms are modeled via an Embedded-Atom-Method interatomic potential which has been tailored to bulk properties [10]. Periodic boundary conditions are imposed in the dislocation line (X in Fig. 1 (a)) and in the dislocation glide direction (Y in Fig. 1 (a)). The size of the simulation box is 130×10 nm in the X and Y directions, respectively, and the thickness is 3.5 nm [The size has been chosen to be several times larger than the Larkin's length]. The upper and lower free surfaces of the system (parallel to the slip) allow us to impose a shear stress σ_{yz} . This translates into a Peach-Koehler force that drags the dislocation through the random crystal above a certain threshold studied in details in [10–12].

The initial configuration is computed with a mere steepest descent gradient algorithm. Due to the relatively weak stacking fault energy of Ni, the dislocation dissociates into two Shockley partial dislocations as expected for face-centered cubic metals (see Fig. 1 (a)). Following this initial relaxation, we apply a constant shear stress (σ_{yz}) and temperature (5 K). The latter is maintained via a Berendsen thermostat.

The dislocation dynamics are analyzed along the trajectories for which the glide distance is at least 150 nm. With the present configuration, the closest stress from the critical depinning transition point is obtained at $\sigma_{yz} = 171.2$ MPa. This order of magnitude is similar to that measured in experiments [13, 14]. The dislocation core is localized by identifying the atoms whose first neighbor cell differs from the perfect crystal. This yields a limit $\ell_x = 0.40$ nm (resp. $\ell_y = 0.58$ nm) in resolution along X (resp. Y). The two partial dislocations move in a coherent manner (see Fig. 1 (a)) due to their strong elastic coupling[12]. As results, we define the effective dislocation position by averaging the two partials. All the analysis thereafter are restricted to the steady state regime, after the dislocation has glided over a distance of 20 nm. Let us finally add that the high-frequency oscillations were removed from the dislocation dynamics and we only considered the forward motions in the statistical analysis presented hereafter.

RESULTS

Morphological scaling features of the time evolving fronts are first characterized. In this context, the height-height correlation functions are computed in both space and time:

$$\begin{aligned}\Delta h(\Delta x) &= \langle (h(x + \Delta x, t) - h(x, t))^2 \rangle^{1/2}, \\ \Delta h(\Delta t) &= \langle (h(x, t + \Delta t) - h(x, t))^2 \rangle^{1/2}\end{aligned}\quad (1)$$

Both are found to exhibit power-law shapes, with exponents $\zeta = 0.85 \pm 0.05$ and $\beta = 0.76 \pm 0.02$, respectively

(Fig. 1 (b): Inset). These scalings are signatures of self-affinity. No lower cutoff is evidenced in space, while the lower cutoff in time appears to be of the order of the inverse of the Debye frequency (7.8 THz in pure Ni). In both cases, the upper cutoffs decay as applied shear σ_{yz} (and hence mean dislocation velocity) increases.

Full spatio-temporal morphological scaling features can be characterized through the computation of the space-time structure function defined as:

$$\Delta h(\Delta x, \Delta t) = \langle (h(x + \Delta x, t + \Delta t) - h(x, t))^2 \rangle^{1/2} \quad (2)$$

As shown in the main panel of Fig. 1 (b), this function is found to obey the Family-Viseck scaling [15]:

$$\Delta h \propto \Delta t^\beta f\left(\frac{\Delta x}{\Delta t^{\beta/\zeta}}\right), \quad f(u) \sim \begin{cases} 1 & \text{if } u \ll 1 \\ u^\zeta & \text{if } u \gg 1 \end{cases}, \quad (3)$$

Such a scaling is expected close to the depinning transition of an elastic manifold. Hence, the exponents ζ , β and $z = \zeta/\beta = 1.12 \pm 0.1$ are identified with the roughness, growth and dynamic exponents, respectively, commonly defined in interface growth problems.

Spatio-temporal intermittent dynamics of the propagating dislocations are now analyzed via a procedure initially proposed in [2] and extensively applied to crack propagation [16, 17] and imbibition [3] problems, among others. It consists: (i) in computing the so-called activity map \mathbf{w} , i.e. the time $w(x, y)$ spent by the dislocation within a small $2.16 \times 2.16 \text{ \AA}^2$ region at each point (x, y) of the glide plane (Fig. 2 (a)); and (ii) in subsequently defining avalanches as clusters of connected points with velocity $v = 1/w$ above $v_c = C\langle v \rangle$ where $\langle \rangle$ denotes averaging over both time and space, and C stands for clip level. The statistics of avalanche area, A , and duration, D , (time elapsed between dislocation arrival and departure in/from the cluster) allow us to characterize quantitatively the intermittent dynamics.

Dislocation propagation just above the depinning threshold ($\sigma_{yz} = 171.2$ MPa) is first considered. Distributions of area A and duration D are presented in Fig.2 (b)-(c). They exhibit power law tails $P(A) \propto A^{-\tau}$ and $P(D) \propto D^{-\alpha}$, as expected in a system near criticality. The two exponents are found to be $\tau = 1.71 \pm 0.03$ and $\alpha = 2.28 \pm 0.1$. Figure 2 (c) reveals also a power-law scaling between area and duration: $D \propto A^\gamma$ with $\gamma = 0.55 \pm 0.03$. Note that τ , α and γ are related: Since D scales as A^γ , the fact that $P(A) \propto A^{-\tau}$ yields $P(D) \propto A^{-(1+(\tau-1)/\gamma)}$ and therefore: $\alpha = 1 + (\tau - 1)/\gamma$. The fulfillment of this relation indicates the high quality of our sampling. Finally, avalanches are shown to exhibit morphological scaling features since their width, L_y , scales as a power-law of their length, L_x (Fig. 2 (e)), with an exponent $H = 0.83 \pm 0.03$. All the scaling exponents described above are found to be robust and independent of clip level.

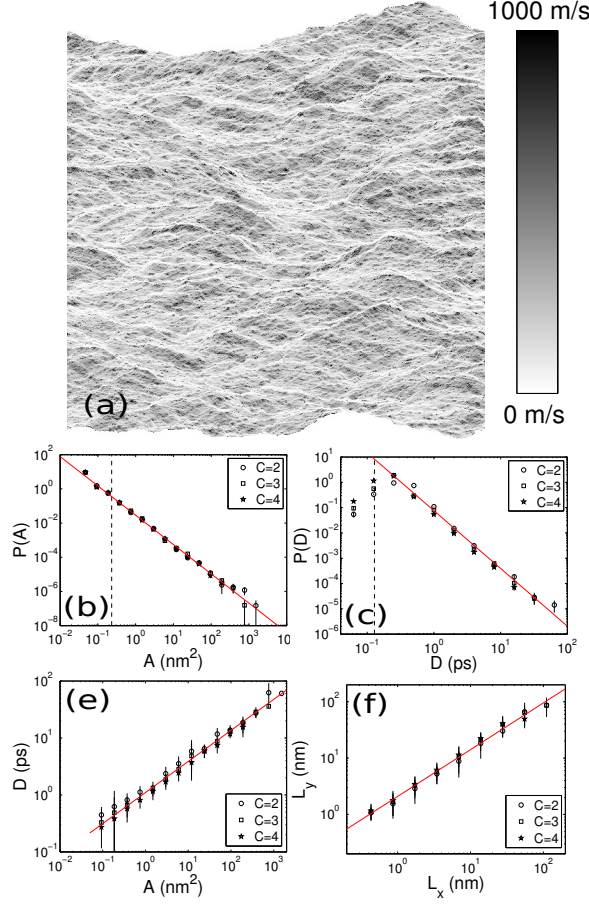


FIG. 2. (Color online) (a) Gray-scale map of velocity matrix obtained in our simulation at $\sigma_{yz} = 171.2$ MPa. (b) Area distribution of avalanches $P(A)$ as defined in the text for different clip levels (see legend). (c) Duration distribution of avalanches $P(D)$ with same clip levels. Error bars are computed as in [18]. (d-e) The scaling of D vs. A and that of avalanche width L_y vs. avalanche length L_x , respectively. In both plots, errorbars indicate the standard deviation. Full lines correspond to power-law fits: $P(A) \propto A^{-\tau}$, $P(D) \propto D^{-\alpha}$, $D \propto A^\gamma$ and $L_y \propto L_x^H$ with $\tau = 1.71 \pm 0.03$, $\alpha = 2.28 \pm 0.1$, $\gamma = 0.55 \pm 0.03$ and $H = 0.83 \pm 0.04$, respectively. The \pm range is defined for a 95% confident interval. The vertical dashed lines correspond to the resolution limits in space and time.

Let us now move to the analysis of the role played by the applied stress σ_{yz} on the dislocation dynamics. The insets in Figs. 3 (a) and (b) show the effect of applied stress on the area and duration distributions, respectively. In both cases, an upper cutoff decreasing with σ_{yz} is observed. Once again, such behaviors are characteristic of a system near criticality. In this context, the distributions are expected to take the form $P(A) = A^{-\tau} f(A/A_0)$ and $P(D) = D^{-\alpha} g(D/D_0)$ where f and g are universal fast decreasing functions, and A_0 and D_0 are the area and duration cutoffs that diverge algebraically as σ_{xy} reaches the critical value. Then, the

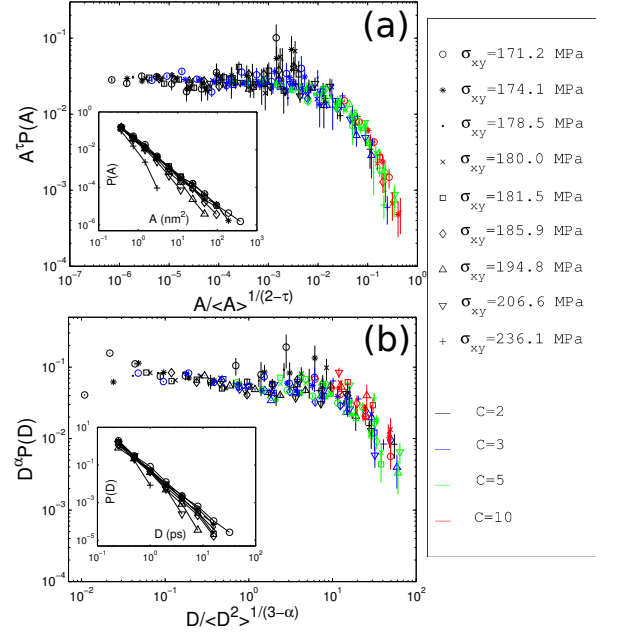


FIG. 3. (Color online) (a) Main panel: Collapsed area distribution obtained from Eq. 4 with $\tau = 1.71$ fitted from data in Fig. 2 (b). Symbols correspond to different clip levels, $C = 2$ (black), $C = 3$ (blue) and $C = 10$ (red) and various σ_{yz} , 171.2 (circle), 174.1 (asterisk), 178.5 (point), 180 (cross), 181.5 (square), 185.9 (diamond), 194.8 (up triangle), 206.6 (down triangle) and 236.1 MPa (plus) according to the right-handed legend. Inset: Avalanche size distribution at $C = 3$ for the different σ_{yz} used in main panel (same symbols). (b) Main panel: Collapsed duration distribution obtained using Eq. 5 with $\alpha = 2.28$ fitted from Fig. 2 (c). Inset: Avalanche duration distribution for fixed clip level $C = 3$ and various σ_{yz} (same values as in (a)).

mean value $\langle A \rangle = \int_0^\infty A \times P(A) dA$ goes as $A_0^{2-\tau}$, and the area distribution can be recast:

$$P(A) = A^{-\tau} f(A/\langle A \rangle^{1/(2-\tau)}). \quad (4)$$

As shown in the main panel in Fig. 3 (a), this scaling is fully verified, and the function f is found to be independent of both σ_{yz} and C over the whole range tested. Note that this analysis must be adapted for durations since $\langle D \rangle = \int_0^\infty D \times P(D) dD$ is not defined when α is larger than two. Instead, the mean value $\langle D^2 \rangle$ is chosen. Since $\langle D^2 \rangle$ goes as $D_0^{3-\alpha}$, one hence expects:

$$P(D) = D^{-\alpha} g(D/\langle D^2 \rangle^{1/(3-\alpha)}). \quad (5)$$

This second scaling is fairly well fulfilled, as demonstrates Fig. 3 (b).

To complete the statistical analysis of dislocation dynamics, we plot in Figs. 4 (a) the variation of $\langle A \rangle$ as a function of σ_{yz} . Once again, the increase of $\langle A \rangle$ as σ_{yz} decreases toward the depinning threshold is reminiscent of a critical behaviour. It is well described by an algebraic divergence of the form $\langle A \rangle \propto (\sigma_{yz} - \sigma_c)^{-\nu_A}$ with

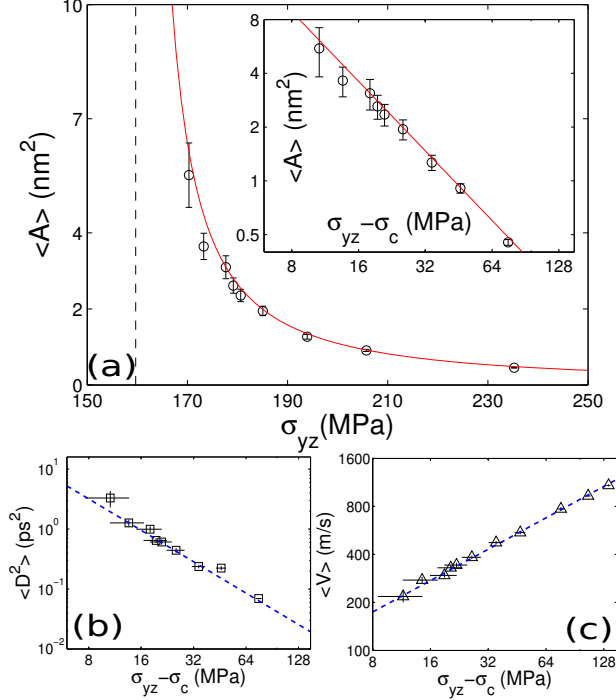


FIG. 4. (Color online) (a) Main panel: Variation of the mean avalanche area $\langle A \rangle$ with applied stress σ_{yz} . Full line is an algebraic divergence $\langle A \rangle \propto (\sigma_{yz} - \sigma_c)^{-\nu_A}$ with fitted parameters $\sigma_c = 159.7 \pm 3$ MPa and $\nu_A = 1.29 \pm 0.05$. Vertical dashed line shows the position of σ_c . Inset: Log-log plot of $\langle A \rangle$ vs $\sigma_{yz} - \sigma_c$. The straight line corresponds to the fit. (b) Log-log plot of the mean value of square duration $\langle D^2 \rangle$ vs. $\sigma_{yz} - \sigma_c$. The straight dashed line is obtained with $\nu_D = 1.75$ from scaling arguments (not fitted). (c) Same as (b) for mean velocity with exponent $\theta = 0.65$ (not fitted).

$\nu_A = 1.29 \pm 0.05$. This divergence in terms of avalanche area translates into a divergence in term of avalanche duration: Since $\langle D^2 \rangle \propto D_0^{(3-\alpha)}$ and $D \propto A^\gamma$, one expects $\langle D^2 \rangle \propto A_0^{\gamma(3-\alpha)} \propto \langle A \rangle^{\gamma(3-\alpha)/(2-\tau)}$ and hence, $\langle D^2 \rangle \propto (\sigma_{yz} - \sigma_c)^{-\nu_D}$ with $\nu_D = \nu_A \gamma (3-\alpha)/(2-\tau) = 1.75 \pm 0.34$. As seen in Fig. 4 (b), this scaling is compatible with direct simulations.

CONCLUDING DISCUSSION

Our analysis of atomic-scale dislocation dynamics in random crystals has revealed many signatures of criticality. To the very best of our knowledge, this work is the first to show that the theoretical framework of second order phase transitions can be applied down to the atomic scales. In this respect, it is of some interest to check the theoretical mapping between the avalanche dynamics extracted from the activity map on one hand, and the revealed morphological scaling features on the other

hand [4]: Avalanches of extent L_x are indeed expected to result from front pieces of extent L_x that depins over a propagating length L_x^ζ and a time $L_x^{1/z}$. Avalanche exponents H and γ are hence expected to be related to ζ and z through $H = \zeta$ and $\gamma = z/(1+\zeta)$ - Both relations are fulfilled in the present atomic scale system.

In the paradigm of critical transitions, the divergence of $\langle A \rangle$ and $\langle D^2 \rangle$ as $\sigma_{yz} - \sigma_c$ vanishes are due to the divergence of a correlation length ξ : $\xi \propto (\sigma_{yz} - \sigma_c)^{-\nu}$. Assimilating ξ to the maximum extent of an avalanche yields $\xi \approx A_0^{1/(1+\zeta)} \propto \langle A \rangle^{1/(1+\zeta)(2-\tau)}$ and hence $\nu = \nu_A/(1+\zeta)(2-\tau) = 2.44 \pm 0.29$. Scaling of the mean dislocation velocity $\langle v \rangle$ can then be deduced: close to σ_c , the propagation is made of avalanches of extent ξ , which moves the dislocation forward by ξ^ζ over a time period ξ^z . Thus, the velocity behaves as $\langle v \rangle \approx \xi^\zeta / \xi^z \propto (\sigma_{yz} - \sigma_c)^\theta$ with $\theta = \nu(z - \zeta)$. This latter relation yields $\theta = 0.65 \pm 0.3$, which is perfectly compatible with the direct measurements (Fig. 4 (c)).

Our system exhibits all signatures expected from the field theory in the vicinity of a critical depinning transition at zero temperature. We can reasonably expect that the predictions of such a theory also apply at finite temperature. In particular, the slow thermally-activated motion of dislocation at low shear stress (below critical threshold) is expected to be given by the creep formula $\langle v \rangle \propto \exp(-U_0(\sigma_c/\sigma_{xy})^\mu/kT)$ where U_0 is a characteristic energy scale and μ a universal exponent [19, 20]. Real deformation experiments actually result from a collective behavior of dislocation involving diverse mechanisms as the interactions with grain boundaries, surfaces, forest dislocations and atomic scale impurities. It seems therefore challenging to demonstrate this in real experiment and atomistic simulation could be a solution.

The present study convincingly shows that the concepts of critical depinning transition apply down to atomic scale. It is worth to mention that the critical exponents measured here do not belong to the standard universality classes associated with the well-established field theories of depinning transition, namely the Edward-Wilkinson (EW)[21], the Kardar-Parisi-Zhang (KPZ)[22] and the Long Range (LR)[23] elastic string models (see Table II). This can be understood since these continuous string models are constructed from symmetries principles by calling upon a *thermodynamic limit* argument (i.e. by making $t \rightarrow \infty$ and $x \rightarrow \infty$ to eliminate the high order derivatives in the equation of string motion), which stops to be relevant at small scales. To understand what determines the universality class at such atomic scales represents a significant challenge for future investigations. Since the field theory of elastic manifold predicts critical behavior in variety of different systems of solid state physics like e.g. domain wall motion in ferromagnets, crack problems, vortex motion in superconductors and charge density wave, etc, it may be of interest to see

whether or not similar extension of criticality down to atomic scale can be evidenced in these systems.

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TABLE I. Depinning exponents obtained directly from simulations and from scaling relations (marked with *)

| | | | |
|--------------------------|-------------------------|----------------------------|---------------------------|
| $\zeta = 0.85 \pm 0.05$ | $\beta = 0.76 \pm 0.02$ | $z = 1.12 \pm 0.1$ | $\theta_* = 0.65 \pm 0.3$ |
| $\nu_* = 2.44 \pm 0.29$ | $\tau = 1.71 \pm 0.03$ | $\alpha = 2.28 \pm 0.1$ | $H = 0.83 \pm 0.04$ |
| $\gamma = 0.55 \pm 0.03$ | $\nu_A = 1.29 \pm 0.05$ | $\nu_{D*} = 1.75 \pm 0.34$ | |

TABLE II. Comparison of the exponents measured in the atomic scale MD simulations reported here with those observed in some well-established scalar field models of elastic line depinning.

| Present study | $\zeta = 0.85 \pm 0.05$ | $\beta = 0.76 \pm 0.02$ | $z = 1.12 \pm 0.1$ | $\nu = 2.44 \pm 0.29$ | $\theta = 0.65 \pm 0.3$ |
|---------------|-------------------------|-------------------------|--------------------|-----------------------|-------------------------|
| EW [24] | $\zeta \simeq 1.26$ | $\beta \simeq 0.84$ | $z \simeq 1.5$ | $\nu \simeq 1.29$ | $\theta \simeq 0.33$ |
| KPZ [25] | $\zeta \simeq 0.633$ | $\beta \simeq 0.633$ | $z \simeq 1$ | $\nu \simeq 1.733$ | $\theta \simeq 0.636$ |
| LR [26] | $\zeta \simeq 0.385$ | $\beta \simeq 0.5$ | $z \simeq 0.77$ | $\nu \simeq 1.625$ | $\theta \simeq 0.625$ |